

# Quasiparticle relaxation dynamics in spin-density-wave and superconducting $\text{SmFeAsO}_{1-x}\text{F}_x$ single crystals

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(Received 7 January 2010; revised manuscript received 11 May 2010; published 3 June 2010)

We investigate the quasiparticle (QP) relaxation and low-energy electronic structure in undoped  $\text{SmFeAsO}$  and near-optimally doped  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  single crystals—exhibiting spin-density wave (SDW) ordering and superconductivity, respectively—using pump-probe femtosecond spectroscopy. In the undoped single crystals a single relaxation process is observed, showing a remarkable critical slowing down of the QP relaxation dynamics at the SDW transition temperature  $T_{\text{SDW}} \approx 125$  K. In the superconducting (SC) crystals multiple relaxation processes are present with distinct SC-state quasiparticle recombination dynamics exhibiting a BCS-like  $T$ -dependent superconducting gap, and a pseudogap (PG)-like feature with an onset above 180 K indicating the existence of a pseudogap of magnitude  $2\Delta_{\text{PG}} \approx 120$  meV above  $T_c$ . From the pump-photon energy dependence we conclude that the SC state and PG relaxation channels are independent, implying the presence of two separate electronic subsystems. We discuss the data in terms of spatial inhomogeneity and multiband scenarios, finding that the latter is more consistent with the present data.

DOI: [10.1103/PhysRevB.81.224504](https://doi.org/10.1103/PhysRevB.81.224504)

PACS number(s): 74.25.Dw, 78.47.J-, 74.25.Gz, 75.30.Fv

## I. INTRODUCTION

The discovery of high-temperature superconductivity in iron-based pnictides (IP) (Refs. 1–3) has attracted a great deal of attention recently. Contrary to the cuprate superconductors, where a single band with a high degree of correlations is believed to be sufficient starting point for the description of the electronic properties, there is a clear theoretical<sup>4</sup> and experimental<sup>5</sup> evidence that in IP several bands cross the Fermi energy ( $\epsilon_F$ ).<sup>6</sup> The implications of the presence of several bands at  $\epsilon_F$  in IP are still under intense investigation. In the undoped state two SDW gaps were detected by optical spectroscopy<sup>7</sup> in 122 compounds ( $\text{AFe}_2\text{As}_2$ ,  $\text{A}=\text{Ba}, \text{Sr}$ ) presumably originating from different bands crossing  $\epsilon_F$ . In  $\text{LaFeAsO}$  (La-1111) a similar optical-conductivity suppression was observed<sup>8</sup> but no analysis in terms of SDW gaps was performed. In the superconducting-state multiple superconducting gaps were detected<sup>9–12</sup> corresponding to different bands crossing  $\epsilon_F$ . In addition to superconducting gaps also the presence of a pseudogap was reported by NMR (Refs. 13 and 14) and point-contact Andreev spectroscopy<sup>15</sup> in La-1111.

Time-resolved spectroscopy has been very instrumental in elucidating the nature of the electronic excitations in superconductors, particularly cuprates, by virtue of the fact that different components in the low-energy excitation spectrum could be distinguished by their different lifetimes.<sup>16–31</sup> Moreover, the relaxation kinetics can give us valuable information on the electronic density of states<sup>17</sup> and electron-phonon coupling.<sup>32</sup> Extensive and systematic experiments on cuprates have also given information on the behavior of the pseudogap for charge excitations, complementing the information obtained on spin excitations from NMR and other spectroscopies.<sup>18,20,26</sup>

In this work we present a time-resolved femtosecond spectroscopy study of undoped and near-optimally doped

$\text{SmFeAsO}_{1-x}\text{F}_x$  single crystals with  $x=0$  and  $x \approx 0.2$ , respectively, with the aim of elucidating the low-energy electronic structure, investigating multicomponent response in superconducting ( $x \approx 0.2$ ) single crystals as a sign of a coexistence of distinct electronic subsystems and to obtain detailed information about the quasiparticle (QP) dynamics in the normal, SDW, and superconducting states.

## II. EXPERIMENTAL

Optical experiments were performed using the standard pump-probe technique with 50 fs optical pulses from a 250 kHz  $\text{Ti}:\text{Al}_2\text{O}_3$  regenerative amplifier seeded with an  $\text{Ti}:\text{Al}_2\text{O}_3$  oscillator. We used the pump photons with either doubled ( $\hbar\omega_p=3.1$  eV) or fundamental ( $\hbar\omega_p=1.55$  eV) photon energy and the probe photons with 1.55 eV photon energy. The pump and probe polarizations were perpendicular to each other and oriented with respect to the crystals to obtain the maximum amplitude of the response at low temperatures. The pump and probe beam diameters were determined by measuring the transmittance of calibrated pinholes mounted at the sample place.<sup>33</sup>

The crystals were flux grown at high pressure at ETH in Zurich<sup>34</sup> and were approximately  $120 \times 80 \mu\text{m}^2$  in size. For optical measurements the crystals were glued on a sapphire substrate mounted in an optical liquid-He flow cryostat.

### A. Undoped, spin-density-wave ordered $\text{SmFeAsO}$

In Fig. 1 we plot temperature dependence of  $\Delta R/R$  transients in undoped  $\text{SmFeAsO}$ . The only discernible difference of the response at different pump-photon energies is the presence of a coherent phonon oscillation with the frequency 5.1 THz ( $170 \text{ cm}^{-1}$ ) at 295 K, at  $\hbar\omega_p=1.55$  eV, which is absent at  $\hbar\omega_p=3.1$  eV, consistent with Raman data.<sup>35</sup> Apart of the

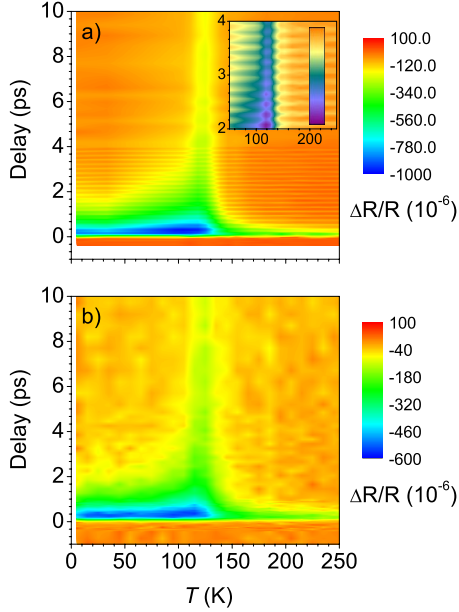


FIG. 1. (Color online)  $\Delta R/R$  transients as a function of temperature at 1.55 eV pump-photon energy and  $18 \mu\text{J}/\text{cm}^2$  (a) and 3.1 eV pump-photon energy and  $15 \mu\text{J}/\text{cm}^2$  (b) in undoped SmFeAsO. In (a) the coherent phonon, shown expanded in the inset, is artificially smeared beyond 4 ps delay due to a decreased time resolution of scans.

coherent phonon oscillation the transients consist of a negative-amplitude single-exponential relaxation with a temperature-independent rise time of  $\sim 180$  fs [see Fig. 2(a)]. Around  $T_{\text{SDW}} \approx 125$  K an additional long-lived response appears with decay time beyond our measurement delay range. The amplitude of the transients,  $A_0$ , linearly increases with decreasing temperature down to  $\sim 170$  K [see Fig. 2(c)] with the relaxation time,  $\tau_{\text{ud}}$ , of  $\sim 220$  fs time changing only weakly above 200 K. Below 200 K  $\tau_{\text{ud}}$  starts to increase while the amplitude starts to depart from the linear dependence only below  $\sim 170$  K rapidly increasing below  $\sim 140$  K, and achieving a maximum at 115 K, upon entering the SDW state. With further decrease in the temperature the amplitude slightly drops at first and then remains constant below 50 K. Simultaneously with the maximum of the amplitude  $\tau_{\text{ud}}$  shows a remarkable divergentlike peak at  $\sim 120$  K and then drops to a temperature independent value of 0.8 ps below 50 K.

The rise and decay times are virtually independent of the fluence,  $\mathcal{F}$ , at all temperatures (see Fig. 3) while the amplitude increases linearly with  $\mathcal{F}$  at 295 K and shows a weak saturation above  $\mathcal{F} = 25 \mu\text{J}/\text{cm}^2$  at 5 K.

### B. Superconducting SmFeAsO<sub>0.8</sub>F<sub>0.2</sub>

The temperature dependence of the  $\Delta R/R$  transients in the near optimally doped sample is shown in Fig. 4. Contrary to the undoped case the transients show complex time and temperature dependencies. Independent of the  $\hbar\omega_p$  one can clearly resolve three temperature regions with different characteristic behaviors.

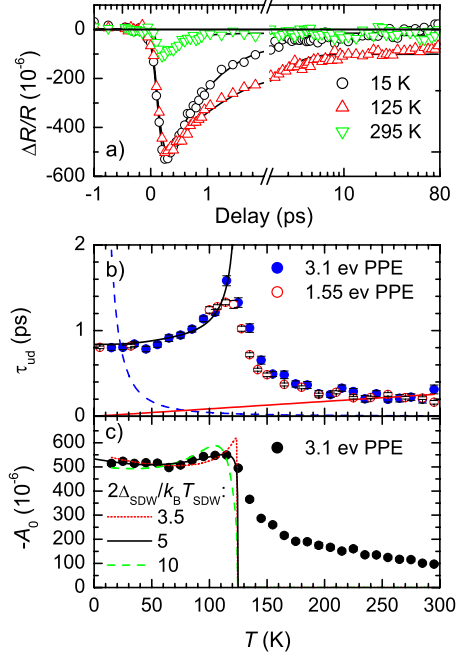


FIG. 2. (Color online)  $\Delta R/R$  transients at representative temperatures in undoped SmFeAsO with single-exponential decay fits (a). (b) The relaxation time at two pump photon energies and (c) amplitude as functions of temperature at  $\mathcal{F} = 15 \mu\text{J}/\text{cm}^2$ . The red solid line in (b) is fit of Eq. (1) to  $\tau_{\text{ud}}$  above 230 K. The blue dashed line in (b) is Eq. (2) with  $\lambda = 0.2$  and  $\Theta_D = 175$  K from Ref. 36. The black thin solid line in (b) represents the fit of Eq. (28) from Ref. 17 discussed in detail in text. Thin lines in (c) represent the fits of Eq. (6) from Ref. 17 with different magnitudes of the gap.

(i) At the high temperatures a negative transient is observed with initial 0.25 ps decay followed by a slower response consisting from a weak peak at 12 ps [see Fig. 5(a)] at  $\hbar\omega_p = 3.1$  eV. The transients scale linearly with increasing fluence except in the region of the initial 0.25 ps decay where a weak  $\mathcal{F}$  dependence is observed at low  $\mathcal{F}$ . At  $\hbar\omega_p = 3.1$  eV the transients have the same shape and similar am-

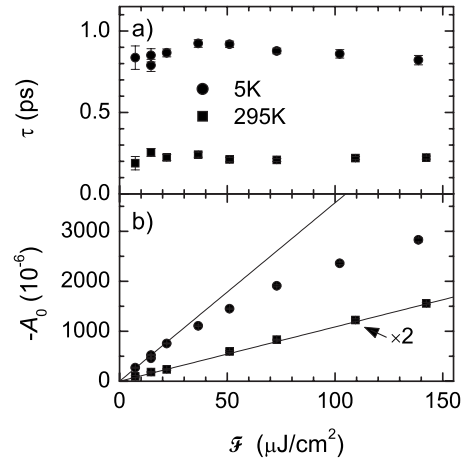


FIG. 3. Fluence dependence of the  $\Delta R/R$  transient amplitude and relaxation time in undoped SmAsFeO at two different temperatures. The thin lines are linear extrapolations of the low fluence data.

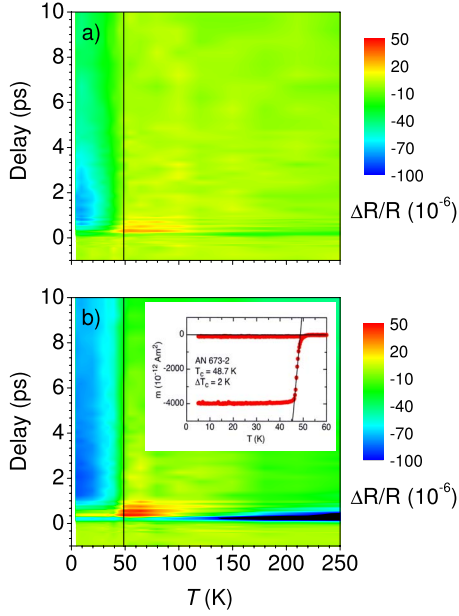


FIG. 4. (Color online)  $\Delta R/R$  transients as a function of temperature at 1.55 eV pump-photon energy (a) and 3.1 eV pump-photon energy (b) in superconducting  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$ . The pump fluence was  $17 \mu\text{J}/\text{cm}^2$  at 3.1 eV and  $15 \mu\text{J}/\text{cm}^2$  at 1.55 eV. Below  $T_c$  the response of the superconducting state is clearly seen. The temperature dependence of the magnetization is shown in the inset.

plitude as in undoped  $\text{SmFeAsO}$  without the coherent phonon. At  $\hbar\omega_p=1.55$  eV the negative high- $T$  transients are much weaker than at  $\hbar\omega_p=3.1$  eV so only the initial 0.25 ps decay is resolved from the noise (see Fig. 6). In addition a coherent phonon is observed with a softer frequency than in undoped  $\text{SmFeAsO}$  of 4.6 THz ( $153 \text{ cm}^{-1}$ ) having similar amplitude at both  $\hbar\omega_p$ .

(ii) At the intermediate temperatures above  $T_c$  and low  $\mathcal{F}$  the transients are positive on the subpicosecond time scale cross zero around 4 ps with the slow dynamics similar to the high-temperature one. At high  $\mathcal{F}$  the positive part of the transients vanishes and the transients become qualitatively identical to those at higher temperatures (see Fig. 5). The only remaining difference is a delay-independent positive vertical shift of the intermediate  $T$  scans with respect to those measured at 250 K and an increased coherent phonon frequency of 5.1 THz ( $170 \text{ cm}^{-1}$ ). The  $\hbar\omega_p=1.55$  eV transients are, as at higher temperatures, similar to the  $\hbar\omega_p=3.1$  eV transients but weaker.

(iii) Below  $T_c$  an additional negative component appears with a rise time of 0.2–0.6 ps, depending on the  $\hbar\omega_p$  and pump fluence, and decay time of  $\sim 5$  ps. The component has a similar amplitude at both  $\hbar\omega_p$ . At high  $\mathcal{F}$  the additional negative component becomes undetectable due to a saturation and the transients become virtually identical to those measured at 55 K including the coherent phonon response.

### III. DISCUSSION

#### A. Undoped $\text{SmFeAsO}$

On cooling, undoped  $\text{LaFeAsO}$  (the most studied material in the Re-1111 IP group) undergoes a sequence of a struc-

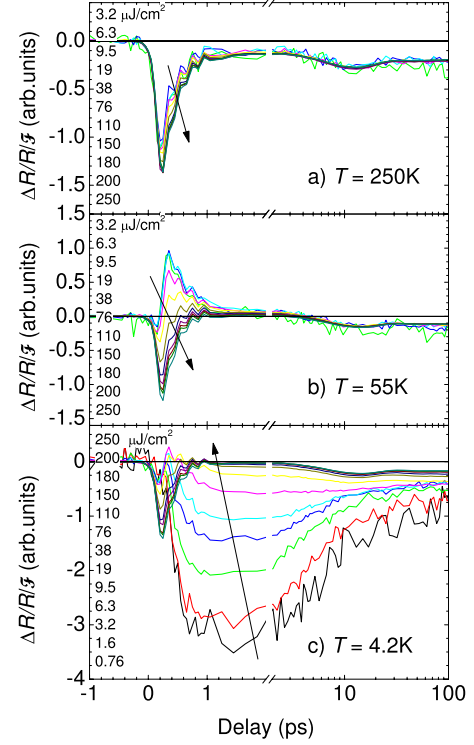


FIG. 5. (Color online) Normalized  $\Delta R/R$  transients at selected temperatures at 3.1 eV pump photon energy as a function of  $\mathcal{F}$  in superconducting  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$ . Above  $\sim 150 \mu\text{J}/\text{cm}^2$  the traces start to overlap indicating a linear  $\mathcal{F}$  dependence. The arrows indicate the direction of increasing  $\mathcal{F}$ .

tural transition from a tetragonal to orthorhombic symmetry, at  $T_s=156$  K, and a magnetic SDW transition at  $T_{\text{SDW}}=138$  K.<sup>37</sup> In  $\text{SmFeAsO}$  the SDW transition was reported at

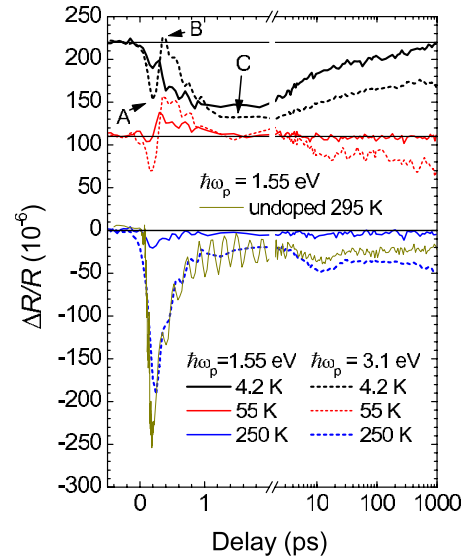


FIG. 6. (Color online)  $\Delta R/R$  transients at different pump-photon energies and selected temperatures in superconducting  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$ . For comparison the 295 K transient from undoped  $\text{SmFeAsO}$  is also shown. The characteristic features due to different components in the superconducting state are shown by arrows.

$T_{\text{SDW}} \sim 135$  K (Ref. 38) while the structural transition was reported at lower temperature  $T_s = 130$  K.<sup>39</sup> So far due to possible different oxygen deficiencies in the two experiments<sup>38,39</sup> and strong doping dependence of both  $T_{\text{SDW}}$  and  $T_s$  it was not possible to reliably distinguish between  $T_{\text{SDW}}$  and  $T_s$  in SmFeAsO. Our data show a marked critical slowing down at 125 K (see Fig. 1) in the form of the long-lived relaxation tail, while the initial picosecond exponential decay time shows a maximum at  $\sim 115$  K. Since the long-lived relaxation tail affects the quality of the single-exponential picosecond fit [see Fig. 2(a)] we cannot reliably identify 115 K as a separate transition temperature. We are therefore unable to differentiate between structural and spin transitions so we will only refer to a single transition temperature  $T_{\text{SDW}} \approx T_s \approx 125$  K in the rest of the paper.

From our data  $T_{\text{SDW}}$  is lower than reported in literature.<sup>38,40</sup> Due to a variable thermal coupling to the sapphire substrate for such small crystals a small decrease in  $T_{\text{SDW}}$  originating from the oxygen deficiency cannot be distinguished from an apparent decrease in  $T_{\text{SDW}}$  due to the laser heating in our samples.

Above  $T_{\text{SDW}}$  undoped pnictides are bad metals with resistivities in the milliohm centimeter range<sup>8,41</sup> and plasma frequency in an  $\sim 1$  eV range.<sup>7,8</sup> The  $\Delta R/R$  transients in this temperature range are therefore attributed to the relaxation of hot electrons in the states near  $\epsilon_F$ . The magnitude of the  $\Delta R/R$  due to the hot electrons relaxation in a metal strongly depends on the particle-hole asymmetry near the Fermi energy and might vary strongly among different materials. In 122 system it appears to be much weaker.<sup>42,43</sup> We analyze the transients in the framework of the recent theoretical results<sup>32</sup> on electron relaxation in metals. The  $\mathcal{F}$ -independent relaxation time warrants use of the low excitation expansion,<sup>32</sup> where in the high-temperature limit the relaxation time is proportional to the temperature,<sup>44</sup>

$$\tau = \frac{2\pi k_B T}{3\hbar \lambda \langle \omega^2 \rangle}. \quad (1)$$

Here  $\lambda \langle \omega^2 \rangle$  is the second moment of the Eliashberg function and  $k_B$  the Boltzman constant. In the low-temperature limit the relaxation time is predicted to diverge at low  $T$  (Ref. 32)

$$\tau = \frac{2\hbar \Theta_D}{\pi^3 \lambda k_B T^2}, \quad (2)$$

where  $\Theta_D$  is the Debye temperature and  $\lambda$  the electron-phonon coupling constant. Since fluctuations toward the SDW state cause the increase in the amplitude and slow down the response below  $\sim 230$  K we fit Eq. (1) to the relaxation time above 230 K only (see Fig. 2). From the fit we obtain  $\lambda \langle (\hbar\omega)^2 \rangle = 135 \pm 10$  meV<sup>2</sup>. If we estimate  $\langle (\hbar\omega)^2 \rangle \approx 25^2$  meV<sup>2</sup> from inelastic neutron data<sup>45</sup> we obtain  $\lambda \approx 0.2$  indicating a rather weak electron-phonon coupling, which cannot explain high  $T_c$  in the doped compound within a single-band BCS model. To check the consistency of the resulting value of  $\lambda$  we plot in Fig. 2(b) also the low- $T$  result [Eq. (2)] indicating validity of the high- $T$  approximation [Eq. (1)] above 230 K.

Owing to the multiband nature of iron pnictides it is possible that due to optical selection rules some bands with possible higher couplings are not directly detected in  $\Delta R/R$  transients. However, at the temperatures of interest the momentum (interband) scattering is expected to be strong resulting in effective averaging of  $\lambda \langle (\hbar\omega)^2 \rangle$  over all the bands.

Below  $T_{\text{SDW}}$  a gap opens at the Fermi surface introducing a bottleneck in the relaxation.<sup>46</sup> The relaxation across a temperature-dependent gap was analyzed by Kabanov *et al.*<sup>17</sup> We use Eq. (6) from Kabanov *et al.*,<sup>17</sup> which describes the photoexcited change in quasiparticle density in the presence of a temperature-dependent gap, to fit the amplitude below  $T_{\text{SDW}} = 125$  K. Using a single SDW gap energy with the BCS temperature dependence and  $2\Delta_{\text{SDW}}/k_B T_{\text{SDW}} \approx 5$  results in a rather good fit to the amplitude temperature dependence [see Fig. 2(c)]. Equation (28) for the relaxation time from Kabanov *et al.*<sup>17</sup> with the same  $\Delta_{\text{SDW}}(T)$  describes well also the temperature dependence of the relaxation time [see Fig. 2(c)]. However, Eq. (28) from Kabanov *et al.*<sup>17</sup> also predicts a fast decrease in the relaxation time with  $\mathcal{F}$ , which is not observed in our data. The reason for this might originate in the fact that the SDW state is not fully gaped and the energy relaxation is not limited by the anharmonic energy transfer from the high-frequency to the low-frequency phonons as assumed in the derivation.<sup>17</sup>

## B. Decomposition of the $\Delta R/R$ transients in superconducting SmFeAsO<sub>0.8</sub>F<sub>0.2</sub> into components

While the transients in the undoped sample show a simple single-exponential relaxation the transients in the doped sample show a clear multicomponent relaxation. To separate contributions from different components we first use<sup>47,48</sup> the fluence dependence of the reflectivity transients. The contributions from the relaxation processes corresponding to the normal state are expected to scale linearly with  $\mathcal{F}$  because the perturbation of a few hundred microjoule per square centimeter is weak for the normal state. On the other hand, the low  $T$ -ordered states are more fragile and can be destroyed by a significantly weaker external perturbation resulting in the saturation with increasing  $\mathcal{F}$ .

It turns out that the data can be consistently described by three distinct components A, B, and C, which are tightly connected with the three observed temperature regions. The temperature-independent linear scaling of the transients with  $\mathcal{F}$  above  $\sim 150$   $\mu\text{J}/\text{cm}^2$  suggests the decomposition of the raw  $\Delta R/R$  into component A which scales linearly with  $\mathcal{F}$  and a *residue* composed from components B and C which saturate at finite  $\mathcal{F}$  (see Fig. 7).

Component A dominates at high temperatures and has to originate in at least three distinct relaxation processes due to the relatively complex time evolution. (i) The slower dynamics, which is virtually the same as in undoped SmFeAsO at high temperatures (see Fig. 6), could be attributed to the band renormalization due to the lattice expansion. (ii) The subpicosecond decay, also having a similar decay time as in undoped SmFeAsO at high temperatures, will be discussed in more detail below. (iii) The oscillatory part of component



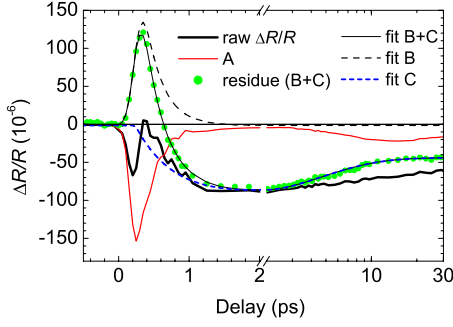


FIG. 7. (Color online) Decomposition of  $\Delta R/R$  transients into different components in the superconducting state in  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$ .

A is attributed to a coherent phonon oscillation which appears softer as in undoped  $\text{SmFeAsO}$ . Except for the shift of the coherent phonon frequency all show only a minor  $T$  dependence.

The *residue* shows a single-exponential decay (see Fig. 8) above  $T_c$ , which we name component B. Component B dominates in the raw transients in the intermediate temperature range, above  $T_c$ . Below  $T_c$  the *residue* changes to a multiexponential decay with the sign change, evidently due to the appearance of an additional relaxation process associated with the superconducting state named component C. Component C saturates at lower  $\mathcal{F} \approx 10 \mu\text{J}/\text{cm}^2$  than component B, which saturates above  $\sim 70 \mu\text{J}/\text{cm}^2$ . The separation of component C from components A and B is further supported by comparison of the raw  $\Delta R/R$  at different  $\hbar\omega_p$  shown in Fig. 6 where components A and B show much smaller amplitudes at  $\hbar\omega_p = 1.55 \text{ eV}$  in comparison to  $\hbar\omega_p = 3.1 \text{ eV}$ , while the amplitude of component C shows a negligible  $\hbar\omega_p$  dependence.

Above  $T_c$  we fit the *residue* with a single-exponential decay (component B)<sup>49</sup> (see Fig. 8),

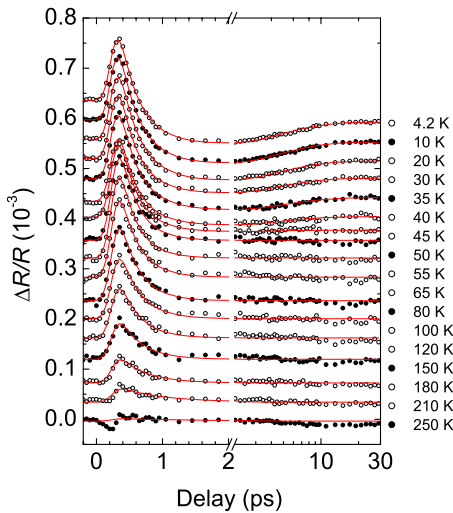


FIG. 8. (Color online) Temperature dependence of  $\Delta R/R$  transients with component A subtracted. Thin lines are single-exponential decay fits of Eq. (3) above  $T_c$  and multiexponential decay fits [a sum of Eqs. (3) and (4)] below  $T_c$ .

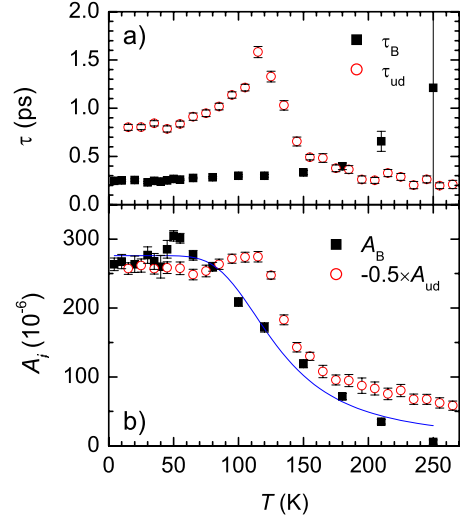


FIG. 9. (Color online) (a) Temperature dependence of the component-B relaxation time and (b) amplitude in superconducting  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  obtained from the fits. The thin line is the fit for the case of a relaxation over a  $T$ -independent gap (Refs. 17 and 47) with  $2\Delta_{\text{PG}} = 120 \text{ meV}$ . For comparison, the temperature dependence of the relaxation time and the transient amplitude in undoped  $\text{SmAsFeO}$  is also shown.

$$\frac{\Delta R_B}{R} = \frac{A_B}{2} e^{-(t-t_0)/\tau_B} \text{erfc}\left(\frac{\sigma^2 - 4(t-t_0)\tau_B}{2\sqrt{2}\sigma\tau_B}\right), \quad (3)$$

where  $\sigma$  corresponds to the effective width of the excitation pulse with a Gaussian temporal profile arriving at  $t_0$  and  $\tau_B$  the exponential relaxation time. Below  $T_c$  additional exponential decays representing component C are needed to fit the *residue*,

$$\begin{aligned} \frac{\Delta R_C}{R} = & A_{1C}(e^{-(t-t_0)/\tau_{1C}} - e^{-(t-t_0)/\tau_{2C}}) \\ & + A_{2C}(e^{-(t-t_0)/\tau_{2C}} - e^{-(t-t_0)/\tau_{3C}}), \end{aligned} \quad (4)$$

where  $\tau_{rC}$  represents the rise time and  $\tau_{iC}$  the decay times.

The resulting fit parameters for component B are shown in Fig. 9. The decay time,  $\tau_{1B} \approx 0.25 \text{ ps}$  at 4 K, slightly increases with increasing temperature below 200 K. Above 200 K, where artifacts due to subtraction of component A start to be significant,  $\tau_{1B}$  steeply increases toward 1 ps. The amplitude of component B,  $A_B$ , stays almost constant up to  $\sim 70 \text{ K}$  and then drops monotonically.

### C. Superconducting response in $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$

For easier separation of component C associated with the superconducting response we use the fact that components A and B are temperature independent in the superconducting state. We therefore extract component C, without relying on the fluence dependence, by subtracting the average of the transients measured at 55 and 65 K from transients measured below 55 K. The subtraction gives the same results as the decomposition based on the fluence dependence. Component C clearly shows a two-step decay with a finite rise time and are excellently fit by Eq. (4) as shown in Fig. 10.

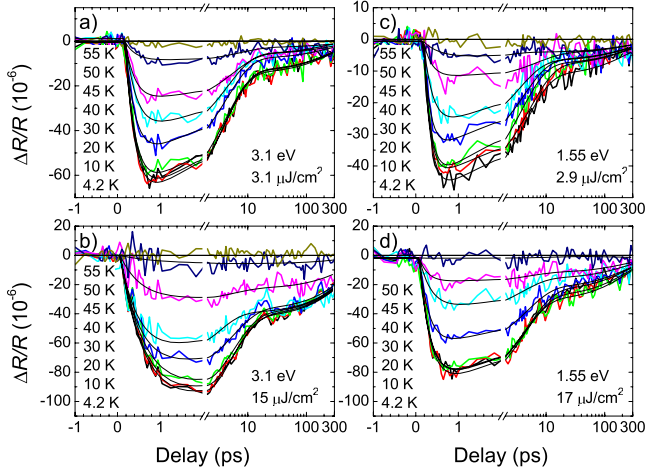


FIG. 10. (Color online) Component C as a function of temperature at different pump photon energies and fluences. Thin lines are fits discussed in text.

In the spirit of the Rotwarf-Taylor model<sup>28</sup> we associate the rise time with establishment of the thermal quasiequilibrium between the photoexcited quasiparticles and high frequency ( $\hbar\omega > 2\Delta_{SC}$ ) phonons. The shorter relaxation time is associated with establishment of the local thermal equilibrium between all degrees of freedom, while the longer relaxation time is due to energy escape out of the probed volume. This is supported by increased relative amplitude of the long decay with respect to the total amplitude at higher  $\mathcal{F}$ .

Neither the rise time nor the relaxation times (see Fig. 11) shows any temperature dependence within experimental error while only  $\tau_{RC}$  shows dependence on  $\mathcal{F}$  and  $\hbar\omega_p$ .  $\tau_{RC}$  is always faster at  $\hbar\omega_p = 1.55$  eV and shows much weaker  $\mathcal{F}$  dependence than at  $\hbar\omega_p = 3.1$  eV, where it increases from 0.3 ps at  $\mathcal{F} = 3 \mu\text{J}/\text{cm}^2$  to 0.6 ps at  $\mathcal{F} = 15 \mu\text{J}/\text{cm}^2$ . While an increase in  $\tau_{RC}$  with increasing  $\hbar\omega_p$  is expected due to the photoexcitation being farther away from  $\epsilon_F$  an increasing  $\mathcal{F}$  dependence with increasing  $\hbar\omega_p$  is not completely understood.

In Fig. 12 we plot  $\mathcal{F}$  dependence of the component C amplitude,  $A_{SC}$ . Similarly as in the cuprates<sup>33</sup> the response saturates with increasing  $\mathcal{F}$  indicating a complete destruction of the superconducting state in the excited volume. By taking into account the effects of inhomogeneous excitation due to finite penetration depths and beam diameters<sup>33</sup> we determine the threshold external fluence,  $\mathcal{F}_T$ , at which the superconductivity is destroyed in the most excited spot of the pump beam. From  $\mathcal{F}_T$  we calculate, using optical penetration depths,  $\lambda_{op}$ , and reflectivities,  $R$ , of  $\text{LaAsFeO}_{1-x}\text{F}_x$ ,<sup>50</sup> the energy density,  $U_p$ , required to completely destroy the superconducting state:  $\frac{U_p}{k_B} = \frac{\mathcal{F}_T(1-R)}{\lambda_{op}k_B} = 2.2 \text{ K/Fe}$  ( $U_p = 18 \text{ J/mol}$ ) at  $\hbar\omega_p = 3.1$  eV and  $\frac{U_p}{k_B} = 1.5 \text{ K/Fe}$  ( $U_p = 12 \text{ J/mol}$ ) at  $\hbar\omega_p = 1.55$  eV. The average value  $\frac{U_p}{k_B} = 1.8 \text{ K/Fe}$  is slightly smaller than the values observed in  $\text{La}_{1-x}\text{Sr}_x\text{CuO}_4$ .<sup>33</sup> If we assume that the thermodynamic superconducting condensation energy,  $U_c$ , in  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  is similar to  $\text{La}_{1-x}\text{Sr}_x\text{CuO}_4$  due to similar magnitudes of  $T_c$  we obtain  $\frac{U_p}{U_c} \gg 1$  indicating that a significant amount of excitation en-

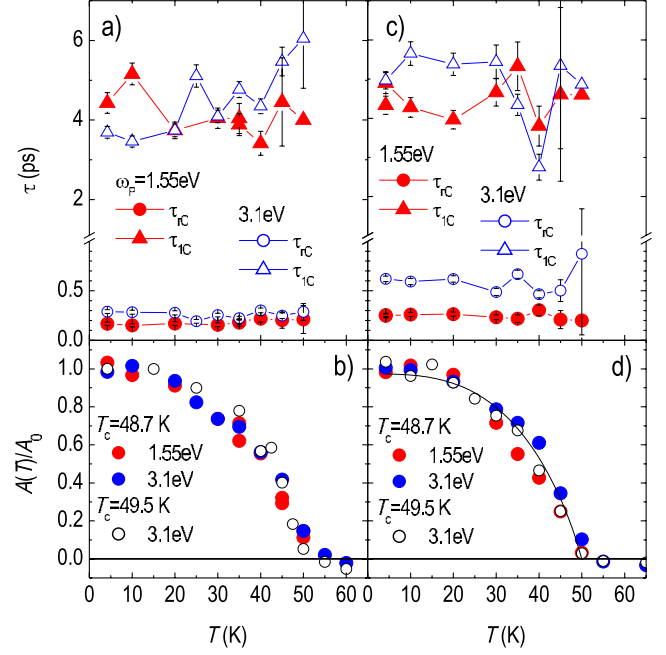


FIG. 11. (Color online) [(a) and (c)] Rise time and relaxation time and [(b) and (d)] amplitude of component C as functions of temperature [(a) and (b)] at  $\mathcal{F} = 2.9 \mu\text{J}/\text{cm}^2$  and  $3 \mu\text{J}/\text{cm}^2$  for  $\hbar\omega_p = 1.55$  eV and 3.1 eV, respectively and [(c) and (d)] at  $\mathcal{F} = 17.4 \mu\text{J}/\text{cm}^2$  and  $15 \mu\text{J}/\text{cm}^2$  for  $\hbar\omega_p = 1.55$  eV and 3.1 eV, respectively. For comparison amplitudes in a slightly higher  $T_c$  sample are shown in (b) and (d). The thin line in (c) is the fit of Eq. (5) to the data.

ergy is transferred to the bath on a timescale of  $\sim 0.3$  ps. If all degrees of freedom would absorb  $U_p$  the resulting temperature rise would be 11 K based on the published heat capacity,  $c_p$ , data.<sup>36</sup> Contrary to the cuprates  $c_p$  is dominated by Sm spins<sup>36,51</sup> below  $\sim 12$  K so it is not possible to determine whether the excess  $U_p$  is absorbed in the Sm spin or in the phonon subsystem.

We fit the temperature dependence of the reflectivity change on complete destruction of the superconducting state shown in Fig. 11(d) by the high-frequency limit of the Mattis-Bardeen formula,<sup>52</sup>

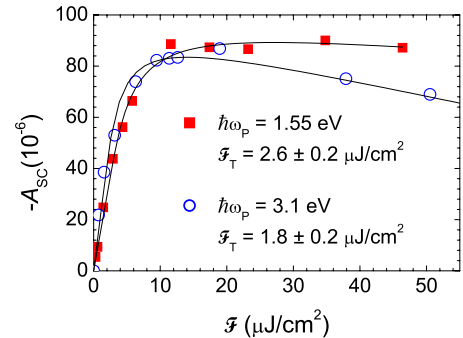


FIG. 12. (Color online) The amplitude of component C as functions of fluence at different  $\hbar\omega_p$ . Thin lines are fits for determination of  $\mathcal{F}_T$  (Ref. 33).

$$\frac{\Delta R}{R} \propto \left( \frac{\Delta(T)}{\hbar\omega} \right)^2 \log \left( \frac{3.3\hbar\omega}{\Delta(T)} \right), \quad (5)$$

where  $\hbar\omega$  is the probe-photon energy and  $\Delta(T)$  the superconducting gap. By using the BCS-gap temperature dependence with  $\frac{2\Delta_0}{k_B T_c} = 3.5$  we obtain an excellent fit to the observed temperature dependence. Unfortunately the shape of the temperature dependence [Eq. (5)] is a very weak function of  $\frac{2\Delta_0}{k_B T_c}$  and one cannot reliably distinguish the contributions from different gaps<sup>53</sup> and reliably determine  $\frac{2\Delta_0}{k_B T_c}$ .

#### D. Normal-state response in SmFeAsO<sub>0.8</sub>F<sub>0.2</sub>

The temperature dependence of the component-B amplitude is consistent with a bottleneck due to the relaxation over a  $T$ -independent gap<sup>17</sup> (see Fig. 9) with a magnitude  $2\Delta_{\text{PG}} = 120$  meV as noted previously.<sup>47</sup> The subpicosecond part of component A on the other hand is temperature independent suggesting a finite density of states at  $\epsilon_F$ . This is consistent with heat-capacity measurements in polycrystalline SmFeAsO<sub>1-x</sub>F<sub>x</sub> (Refs. 36 and 51) where a finite Sommerfeld constant in the superconducting state suggests a finite density of states at  $\epsilon_F$ . Due to very similar pump-photon energy dispersion of components A and B (see Fig. 6) we believe that they originate from the same electronic states which develop a soft-gapped density of states at  $\epsilon_F$  when temperature is decreased. Saturation of component-B amplitude with increasing  $\mathcal{F}$  indicates that the pseudogap can be destroyed so it is not a simple band-structure effect.

The pump-photon energy dispersion similar to that of components A and B is not observed for component C. Electronic states involved in the relaxation related to components A and B must therefore be different than for component C. This confirms that the relaxation below  $T_c$  does *not* proceed via a cascade but rather through distinct parallel channels as suggested previously.<sup>47</sup> These channels correspond to two distinct electronic subsystems which are weakly coupled on the subpicosecond timescale. One exhibits the superconducting gap(s) and the other a pseudogap.

A possible origin of the distinct electronic subsystems could be a chemical phase separation of the doped F. However, the superconducting transition is rather narrow (see Fig. 4) so the presence of weakly superconducting fluorine-poor regions in which SDW is suppressed giving rise to additional pseudogapped electronic subsystem is also unlikely. More importantly undoped SmFeAsO shows virtually no pump-photon energy dispersion which the superconducting sample does, so a simple chemical phase separation to doped and undoped regions is very unlikely despite similarity (see Fig. 6) between component A and the undoped SmFeAsO room-temperature transients. Moreover, there is no divergent signal at 125 K (or anywhere near that temperature) which can be attributed to the presence of the undoped phase in the superconducting sample. We therefore believe that both electronic subsystems are intrinsic to the SC material.

Apart from the chemical phase separation an intrinsic electronic phase separation akin to that proposed for the cuprates<sup>54</sup> could be origin of the distinct electronic subsystems. The existence of intrinsic electronic phase separa-

tion has been reported in 122 systems,<sup>55,56</sup> however, at present the issue is still rather controversial.

In the case of the spatially homogeneous electronic state different electronic subsystems would correspond to different bands crossing  $\epsilon_F$ . This would imply that the interband scattering between parts of the Fermi surface corresponding to different electronic subsystems is negligible on a timescale of a few hundred femtosecond, since excitation photon at 1.5 eV only weakly excites components A and B. Further, since both components exist in the superconducting state even at low  $\mathcal{F}$  the part of the Fermi surface corresponding to components A and B has to remain ungapped or pseudogapped in the superconducting state.

Another possibility for a weakly coupled electronic subsystem is Sm crystal-field levels. The energy of the levels in SmFeAsO<sub>1-x</sub>F<sub>x</sub> is in the range of 20–60 meV as determined indirectly from heat-capacity fits.<sup>57,58</sup> Involvement of the crystal-field levels could explain the strong  $\hbar\omega_p$  dependence of components A and B and decoupling from the other low-lying electronic states. However, the observation of a pseudogap by NMR in La-1111 (Refs. 13 and 14) (which has no crystal-field level structure at low energy), and the weak  $\hbar\omega_p$  dependence in undoped SmFeAsO point against such a scenario.

Finally, let us briefly compare our results in Sm-1111 to femtosecond spectroscopy in (Ba,K)-122.<sup>42,59</sup> There is a marked difference in the magnitude of the relaxation time in the superconducting state, which increases with decreasing temperature beyond 60 ps in optimally doped (Ba,K)-122 (Ref. 42) and remains  $T$  independent in Sm-1111 at  $\sim 5$  ps. Similarly, the excitation fluence dependence of the relaxation time, which is absent in Sm-1111 is pronounced in (Ba,K)-122.<sup>59</sup> This suggests different relaxation mechanisms in Sm-1111 and (Ba,K)-122. While behavior in (Ba,K)-122 is consistent with the Rotwarf-Taylor model<sup>28,60</sup> where the anharmonic optical-phonon decay is determining the relaxation time in Sm-1111 the presence of the ungapped electronic subsystem seems to provide a competing relaxation channel. However, only  $\hbar\omega_p = 1.55$  eV was used in (Ba,K)Fe<sub>2</sub>As<sub>2</sub> so ultrafast pump-probe spectroscopy at different  $\hbar\omega_p$  in 122 systems and measurements in LaFeAsO<sub>1-x</sub>F<sub>x</sub> are needed for determination whether some fundamental difference between 1111 and 122 systems is responsible for the different relaxation-time behavior and marked temperature dependence above  $T_c$  in Sm-1111.

#### IV. SUMMARY AND CONCLUSIONS

In undoped SmFeAsO a single-exponential relaxation of the photoinduced reflectivity transients is observed. From the high- $T$  relaxation time the second moment of the Eliashberg function is determined to be  $\lambda \langle (\hbar\omega)^2 \rangle = 135 \pm 10$  meV<sup>2</sup>. The coupling constant  $\lambda \approx 0.2$ , estimated from this value, is comparable to low- $T_c$  superconductors and cannot explain the high superconducting  $T_c$ 's of these compounds within a single-band BCS model.

Below  $T_{\text{SDW}}$  the temperature dependence of the relaxation indicates appearance of a QP relaxation bottleneck due to opening of a single-charge gap at  $T_{\text{SDW}}$  with a BCS-like

temperature dependence and the amplitude of  $2\Delta_{\text{SDW}}/k_{\text{B}}T_{\text{SDW}} \approx 5$  at 4.2 K. A question whether this charge gap is a direct consequence of the SDW formation or due to the structural transition unfortunately cannot be answered from our data.

In superconducting  $\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  three distinct relaxation components are observed. Components A and B are present in both the superconducting and the normal state. The temperature dependence of the amplitude of component B suggests the presence of a temperature-independent pseudogap with a magnitude  $2\Delta_{\text{PG}} \approx 120$  meV. The pseudogap is destroyed at a finite fluence indicating that it is not a band-structure effect (such as a 120 meV gap at some arbitrary point in the Brillouin zone). Component C is observed only in the superconducting state and corresponds to the relaxation across a  $T$ -dependent superconducting gap with a BCS temperature dependence. At high-enough pump fluence a complete destruction of the superconducting state is observed with the critical optical excitation density  $\frac{U_{\text{p}}}{k_{\text{B}}} \approx 1.8$  K/Fe which is similar to the value observed in  $(\text{La},\text{Sr})\text{CuO}_4$ .

The multicomponent relaxation in SC samples strongly suggests the presence of two relatively weakly coupled electronic subsystems, one exhibiting the SC gap(s) and the other the pseudogap. From the temperature and fluence dependence of photoinduced optical reflectivity transients in undoped and near-optimally doped  $\text{SmFeAsO}_{1-x}\text{F}_x$  single crystals it is clear that the presence of two electronic subsystems in the superconducting sample is not a result of a simple phase separation. The fact that no relaxation component—such as appears in the SDW phase—is seen in the SC phase appears to rule this out. The presence of two electronic subsystems therefore originates either in an intrinsic phase separation or more likely in the multiband nature of the superconducting iron pnictides.

### ACKNOWLEDGMENTS

This work has been supported by ARRS (Grant No. P1-0040) and the Swiss National Science Foundation NCCR MaNEP.

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